

# Numerical Analysis of Aluminum Alloy Reticulated Shells with Gusset Joints under Fire Conditions

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## Abstract

This paper conducts numerical analysis on aluminum alloy reticulated shells (AARSs) with gusset joints under fire conditions. Firstly, the thermal-structural coupled analysis model of AARSs considering joint semi-rigidity is proposed and validated against the room-temperature and fire tests. The proposed model can also be adopted to analyze the fire response of other reticulated structures with semi-rigid joints. Secondly, parametric analysis is carried out based on the numerical model to explore the buckling behavior of K6 AARS with gusset joints under fire conditions. The results indicate that the span, height-to-span ratio, height of the supporting structure, and fire power are influential in the reduction factor of the buckling capacity of AARSs under fire conditions. In contrast, the reduction factor is independent of the number of element divisions, the number of rings, the span-to-thickness ratio, and the support condition. Subsequently, practical design formulae for predicting the reduction factor of buckling capacity of K6 AARSs are derived based on numerical analysis results and machine learning techniques to provide a rapid evaluation method. Finally, further numerical analyses are conducted to propose practical design suggestions, including the conditions of ignoring the ultimate bearing capacity analysis of K6 AARSs and ignoring the radiative heat flux.

## Keywords

aluminum alloy reticulated shell, gusset joint, numerical analysis, fire resistance

## 29 1 Introduction

30 Aluminum alloys are increasingly applied in large-space spatial structures owing to  
31 their advantages of corrosion resistance, high strength-to-weight ratio, and favorable  
32 appearance. As one of the most popular structural types of aluminum alloy structures,  
33 single-layer reticulated shells can have multiple and even complex structural forms to  
34 adapt to aesthetic requirements, e.g., spherical shells, cylindrical shells, and free-form  
35 shells. Hence, traditional fire design concerning the resistance of structural components  
36 may not be economical [1]. In order to resolve this problem, the concept of  
37 performance-based fire resistance design is proposed, which calls for evaluation of the  
38 structural performance objectives, e.g., resistance or residual deformation of a specific  
39 structure or its structural components, under the designed fire scenarios.

40 Large-space fires differ from compartment fires since the volume of the fire is  
41 significantly smaller than that of the interior space, and the air temperature cannot be  
42 regarded as uniformly distributed. Hence, a large-space fire scenario firstly generates a  
43 non-uniformly distributed air temperature field. Then, the structural components  
44 receive the heat flux from the air and the fire through heat convection and radiation.  
45 Finally, the thermal expansion and changes in material properties cause the responses  
46 of the structure. Therefore, the performance-based fire resistance design for large-space  
47 fire scenarios requires data, including the air temperature field, the temperature  
48 development of structural components, and the structural response.

49 Conducting fire tests is the most direct way to obtain the data mentioned above.  
50 Despite the fire tests on different types of steel structures [2–8], fire tests on aluminum  
51 alloy structures have also been carried out in recent years. Guo *et al.* [9] conducted fire  
52 tests on a scale single-layer spherical aluminum alloy reticulated shell (AARS), where  
53 8 large-space fire scenarios were designed. No damage to the shell specimen was  
54 observed after the fire tests, and the structural displacement was proved elastic. Then,  
55 Zhu *et al.* [10] proceeded with 2 destructive tests on the same shell specimen. The  
56 failure mode of the shell specimen under the designed fire scenario was the collapse,  
57 and the structural components failed by melting, rupture, and flexural-torsional  
58 buckling. As the aforementioned 2 studies focused on spherical reticulated shells, Yin  
59 *et al.* [11] designed a full-scale fire test on a cylindrical AARS specimen to evaluate the  
60 air temperature field. The test results revealed that the critical air temperature when the  
61 specimen collapsed was 330 °C, indicating that the existing suggestion on the critical  
62 temperature limit, i.e., 150 °C, has a large safety of margin.

63 Although fire tests can produce immediate data, they consume considerable time  
64 and resources. As the fire tests conducted in references [9–11] all recorded the thermal  
65 or structural responses of the specimen, it is possible to simulate the fire process using

66 numerical analysis, including the air temperature field, the temperature development of  
67 the structural components, and the global structural response. Regarding the simulation  
68 of the air temperature field, references [9] and [11] used the field simulation software  
69 FDS and the existing empirical formula proposed by Du and Li [13]. The comparison  
70 indicated that the field simulation can produce a relatively accurate prediction of the air  
71 temperature field, yet the parameters in the empirical formula should be reasonably  
72 adjusted. As for the simulation of temperature development of aluminum alloy  
73 structural components, Zhu *et al.* [14] proposed an iterative calculation method and  
74 highlighted that the radiative heat flux produced by the fire in large-space fire scenarios  
75 cannot be ignored. Nonetheless, the simulation method of the structural response of  
76 aluminum alloy structures, i.e., the thermal-structural coupled analysis method, has not  
77 been proposed, which dramatically interferes with the performance-based fire  
78 resistance design process and the promotion of aluminum alloy structures. Notably,  
79 typical joint systems of aluminum alloy structures, such as the gusset joint system, are  
80 usually semi-rigid [15–18], and their semi-rigidity has been proved to be influential to  
81 the structural performance under room temperature [19]. However, the numerical model  
82 established for AARSs under room temperature [20, 21] cannot be directly applied to  
83 fire analysis since a temperature-dependent variation of the joint rigidity is included  
84 [22].

85 In addition, it is notable that in the performance-based fire resistance design, the  
86 field simulation and the thermal-structural coupled analysis are computationally  
87 expensive and are not friendly to practical engineers at the initial/concept design stage.  
88 Specifically, repeated thermal-structural coupled analyses are needed if the cross-  
89 sections of the members are adjusted, and additional field simulations are included if  
90 the fire scenario is adjusted due to changes in the architectural composition. The above  
91 problems call for rapid evaluation methods and practical design suggestions to provide  
92 valuable information for designers at the initial/concept design stage.

93 This paper conducts numerical analysis on AARSs with semi-rigid gusset joints  
94 under fire conditions. Firstly, the numerical model of AARSs under room temperature  
95 and its restrictions are briefly reviewed. Secondly, the numerical model for fire analysis  
96 is proposed and validated against the fire test data. Then, parametric analysis of the  
97 ultimate bearing capacity of K6 AARSs under fire conditions is conducted based on the  
98 validated thermal-structural coupled analysis model, and corresponding mechanisms  
99 are analyzed. Practical design formula for predicting the ultimate bearing capacity of  
100 K6 AARSs is proposed based on further numerical analysis and machine learning  
101 techniques. Finally, practical design suggestions, including the conditions of ignoring  
102 the ultimate bearing capacity analysis of K6 AARSs, and conditions of ignoring the

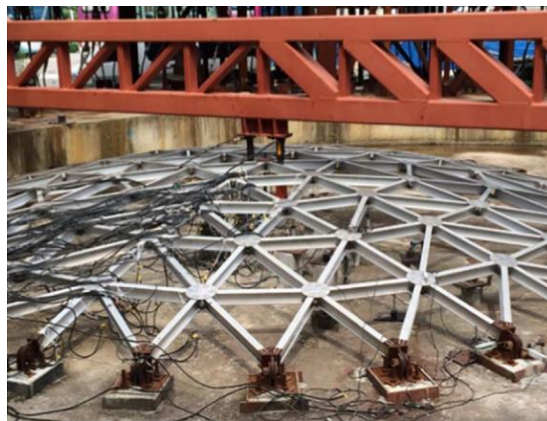
103 radiative heat flux, are proposed based on further numerical analysis.

104

## 105 **2 Numerical model**

### 106 **2.1 Model at room temperature and its restrictions**

107 Based on a room-temperature static experiment on a K6 AARS specimen with semi-  
108 rigid gusset joints shown in Fig. 1 [23], Xiong *et al.* [20] established and verified the  
109 numerical model to simulate the stability behavior of the specimen using the general  
110 finite element software ANSYS [25]. In the numerical model, the BEAM188 element  
111 is used to simulate the member and the joint zone. It is noteworthy that due to the  
112 existence of the joint plate, the out-of-plane bending stiffness of the joint zone is  
113 significantly larger than that of the member. Thus, the elastic modulus of the element at  
114 the joint zone is set as  $100E$ , where  $E$  is the elastic modulus of the member. Note that  
115 the value of 100 is determined based on trial and error [20]. The two-node non-linear  
116 spring element COMBIN39 is used to simulate the out-of-plane bending stiffness of the  
117 gusset joint, where the non-linear stiffness parameters are calculated by the four-line  
118 model proposed by Guo *et al.* [26]. In order to save the computational cost, the other  
119 degrees-of-freedom (DOFs), including the 3 translational DOFs, the in-plane, torsional  
120 rotational DOFs, and the warping DOF, are coupled between the member and the joint  
121 zone.



122

123 **Fig. 1** Room-temperature static test specimen of a K6 AARS [23].

124 Through experimental and numerical investigation, Guo *et al.* [22] highlighted that  
125 the rigidity of the gusset joint is dependent on the temperature. However, the real  
126 constants of the COMBIN39 element, i.e., the out-of-plane bending stiffness of the joint,  
127 cannot be varied through the analysis directly or indirectly, e.g., via the birth and death  
128 element method. Therefore, the numerical model under room temperature cannot be  
129 directly applied to fire analysis.

130

131 **2.2 Numerical model for fire analysis**

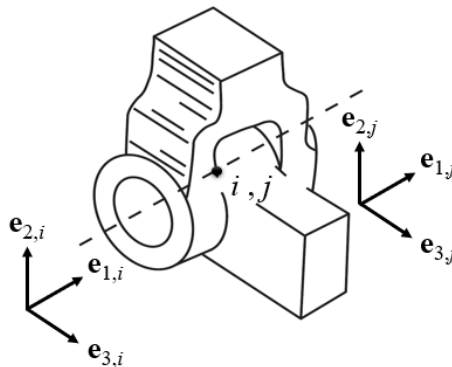
132 In order to consider the temperature-dependent joint rigidity, the MPC184 element,  
 133 which is a multi-point constraint element based on the Lagrange multiplier method, is  
 134 used to replace the COMBIN39 element in the room-temperature numerical model. In  
 135 specific, the pin sub-element shown in Fig. 2 is adopted. The pin sub-element is a two-  
 136 node single-degree-of-freedom element, which can rotate around axis 1 of the local  
 137 coordinate system of nodes  $i$  and  $j$ . In Fig. 2,  $\mathbf{e}_{m,i}$  and  $\mathbf{e}_{m,j}$  are the unit vectors of nodes  $i$   
 138 and  $j$  in the  $m$  direction ( $m = 1, 2, 3$ ) of their local coordinate systems, respectively.  
 139 Denote  $\mathbf{u}_i$  and  $\mathbf{u}_j$  as the resultant displacement vectors of nodes  $i$  and  $j$ , respectively, and  
 140 the constraint conditions of the pin element can be described as

$$141 \quad \begin{cases} \mathbf{u}_i = \mathbf{u}_j \\ \mathbf{e}_{1,i} \cdot \mathbf{e}_{2,j} = 0 \\ \mathbf{e}_{1,i} \cdot \mathbf{e}_{3,j} = 0 \end{cases} \quad (1)$$

142 The non-linear stiffness, damping properties, and Coulomb friction of the pin element  
 143 at different temperatures can be simulated by defining the material properties. The  
 144 element also supports geometric non-linear analysis and linear perturbation analysis.

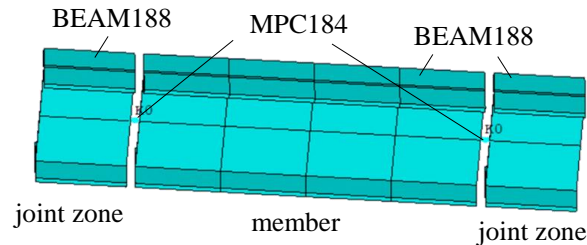
145 When using the pin sub-element of the MPC184 element to simulate the non-linear  
 146 bending stiffness of the gusset joint, the following points should be noted:

- 147 (1) The two nodes of the element must have the same spatial coordinates;
- 148 (2) After defining an element, the SECDATA command must be used to define a  
 149 shared local coordinate system for both nodes;
- 150 (3) Use the JOIN option in the TB command to define the non-linear moment-  
 151 rotation curve of the joint, and input the points on the curve by the TBDATA  
 152 command;
- 153 (4) Use the TBTEMP command to shift different temperatures for the moment-  
 154 rotation curves.



155 **Fig. 2** Pin sub-element of the MPC184 element [25].

157 Therefore, the simplified numerical model for a member in AARSs is established  
 158 as shown in Fig. 3, where the elements selected for the member and the joint zone are  
 159 the same as described in Section 2.1. Note that we do not consider the stiffness reduction  
 160 of the joint zone due to the elevated temperature, as no joints fail before the members  
 161 in the fire test conducted in literature [10].



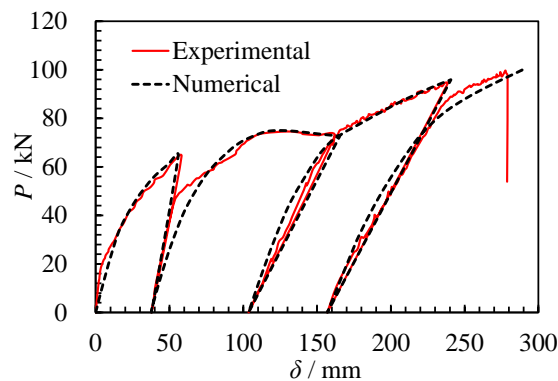
162  
 163 **Fig. 3** Simplified numerical model for a member in the AARS.

164  
 165 **2.3 Validation of the model for fire analysis**

166 As the proposed numerical model for fire analysis is adaptive to the bending stiffness  
 167 of the joint under different temperatures, this section verifies the model using the room-  
 168 temperature test data [23] and the fire test data [10].

169 a) Room-temperature test

170 Fig. 4 shows the comparison of the load-displacement curve of the top joint of the  
 171 shell specimen obtained by the experimental data and the proposed numerical model,  
 172 where  $P$  is the load and  $\delta$  is the vertical displacement. As the curve obtained by the  
 173 proposed model is in good agreement with the experimental curve, it can be concluded  
 174 that the proposed numerical model is also reliable in simulating the buckling behavior  
 175 of reticulated shells with semi-rigid joints at room temperature.

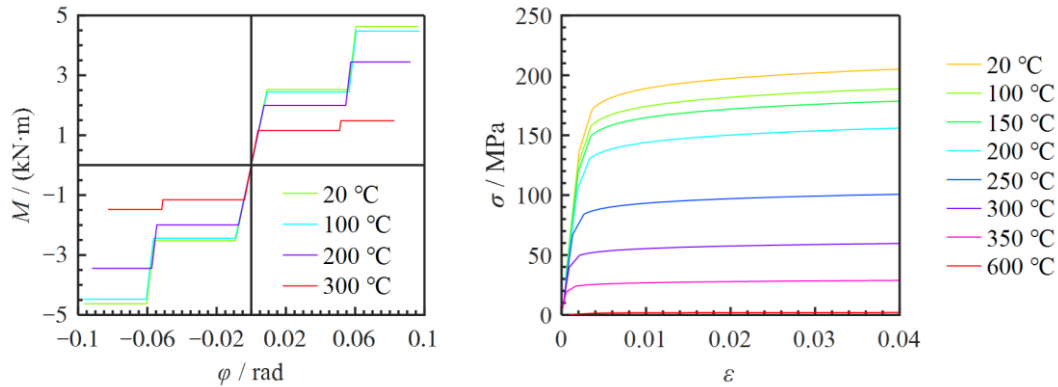


176  
 177 **Fig. 4** Comparison of load-displacement curves obtained by test and numerical simulation.

178 b) Fire test

179 Fig. 5 (a) plots the material constitutive model of the 6063-T5 aluminum alloy used  
 180 for the AARS specimen in reference [10]. Notably, the elastic modulus and nominal

181 yield strength of the material at 600°C are set as 1% of those under room temperature  
 182 to simulate the melting of the material. Based on the out-of-plane bending stiffness  
 183 model of aluminum alloy gusset joints at elevated temperatures [22], the out-of-plane  
 184 moment-rotation curves of the joints in the AARS specimen [10] at different  
 185 temperatures are calculated as shown in Fig. 5(b). Note that the elevated-temperature  
 186 constitutive model shown in Fig. 5(b) is determined by the room-temperature tensile  
 187 test conducted in literature [10], the elevated-temperature material property reduction  
 188 factors, and constitutive models recommended in the Eurocode 9 [24].



189

(a) Material constitutive model

(b) Out-of-plane bending stiffness of the joint

190

**Fig. 5** Properties of material and joint in the AARS shell specimen tested in literature [10] at  
 191 different temperatures  
 192

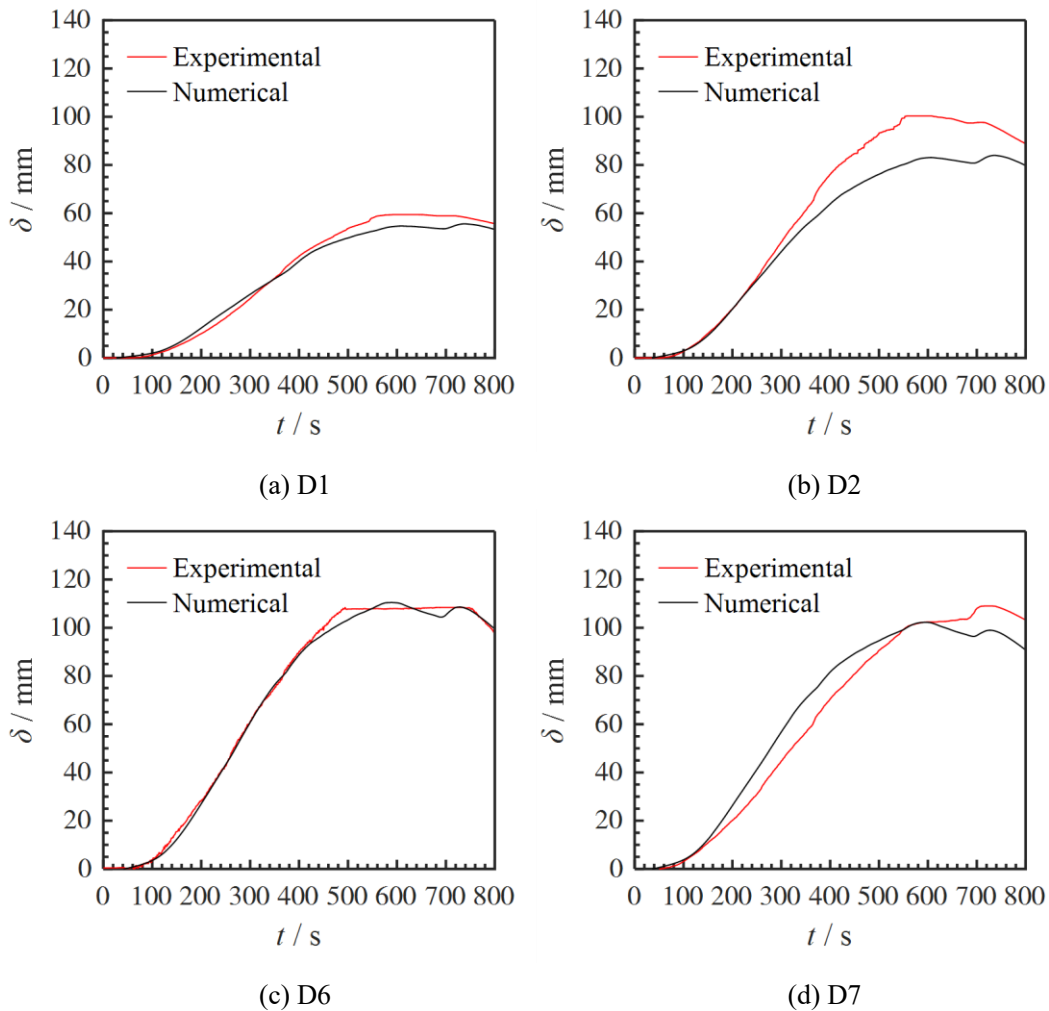
193 Destructive fire tests D-1 and D-2 in reference [10] are used for validating the  
 194 established numerical model since the deformation of the specimen is large. The stable  
 195 combustion state of the two tests is exhibited in Fig. 6. By introducing the measured  
 196 member temperature data to the numerical model, the comparison of the experimental  
 197 and numerical displacement-time curves of typical joints in the AARS specimen in fire  
 198 tests D-1 and D-2 [10] are shown in Figs. 7 and 8, respectively, where the upward  
 199 displacement is positive. Note that  $D_i$  is the symbol of the  $i$ th displacement transducer,  
 200 whose detailed location is given in reference [10]. Besides, only the displacement  
 201 curves before the fire became very faint in test D-1 are introduced in Fig. 7, i.e., the  
 202 time range is 0 s ~ 800 s. The comparison of the numerical and experimental  
 203 deformation of the specimen is shown in Fig. 9. It can be concluded from the good  
 204 agreement of the curves and the identical deformation patterns that the proposed  
 205 numerical model is able to simulate the thermal expansion, stiffness degradation, and  
 206 the fire-induced collapse of AARS with semi-rigid gusset joints. Notably, the numerical  
 207 simulation of test D-2 is terminated at the end of the test, i.e., at 614 s, while the photo  
 208 shows the ultimate deformation when the fire is finally extinct. Although there are slight  
 209 differences, it can still be concluded that the sinking deformation at the center of the  
 210 specimen within the fire duration has been well simulated.

211 The proposed model can also be used to simulate the buckling behavior of other  
 212 types of reticulated structures with semi-rigid joints under fire conditions when  
 213 different bending stiffness models are introduced for the MPC184 element.



214  
 215  
 216

**Fig. 6** Stable combustion state of the two fire tests used for validation [10]



217  
 218

**Fig. 7** Comparison of experimental and numerical displacement-time curves of typical joints in test D-1

223 As the readings of the displacement sensors have been reset to zero before tests D-  
 224 1 and D-2, the displacement induced by the vertical load applied before the tests will  
 225 not influence the comparison shown in Figs. 7 and 8.



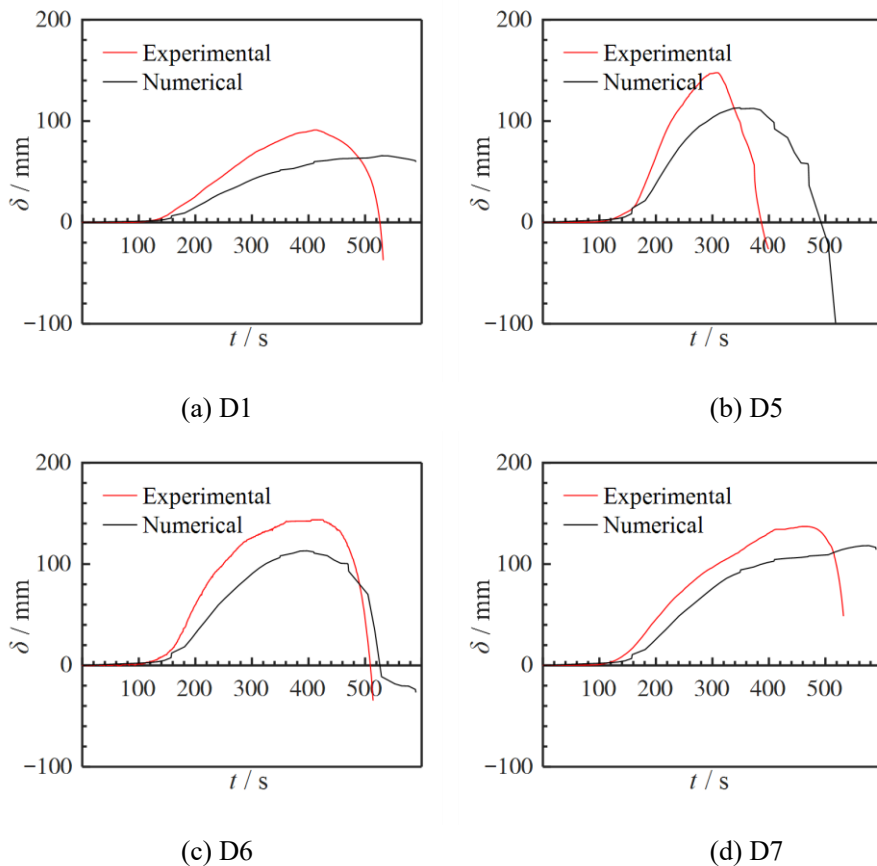
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### 227 3 Parametric study

228 Zhu *et al.* [10] analyzed the mechanism of the fire-induced collapse of K6 AARSs. They  
229 concluded that the *ferrule effect* is the main cause of the thermal compressive forces of  
230 the ring members. The failure of the structure is the outcome of degradation of material  
231 properties, the ferrule effect, and the catenary action.

232 As the K6 reticulated shell is one of the most commonly-used spatial structural  
233 types, this section further investigates the ultimate bearing capacity of K6 AARS with  
234 gusset joints under fire conditions, based on the proposed numerical model. The main  
235 motivation is that the ultimate bearing capacity of the structure is also concerned in the  
236 performance-based fire resistance design. In order to illustrate the variation in the  
237 ultimate bearing capacity during the fire process, we define  $k_{\Lambda}(t)$  as the reduction factor  
238 of the ultimate bearing capacity at time  $t$  of the fire process, calculated by

$$239 \quad k_{\Lambda}(t) = \frac{\Lambda(t)}{\Lambda(0)} \quad (2)$$



240

241

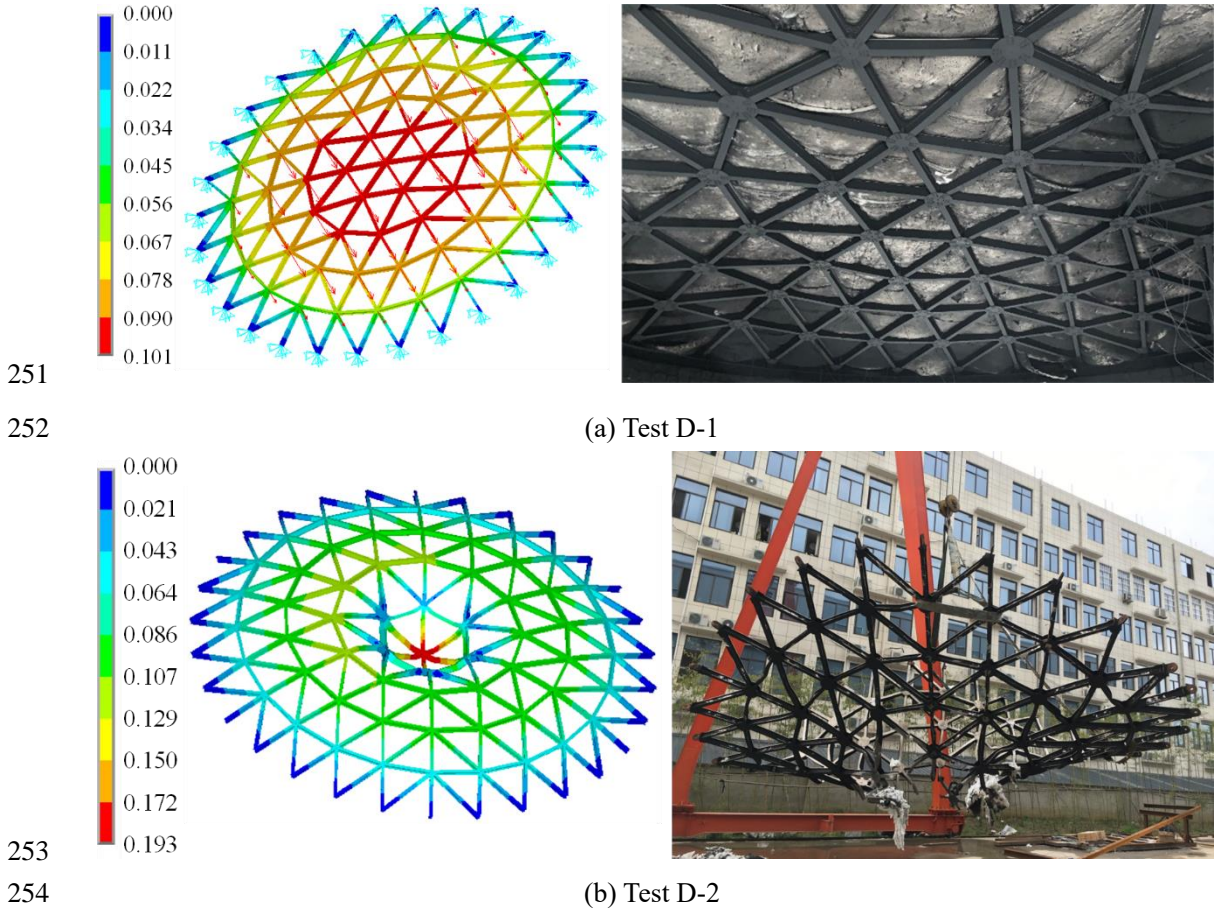
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243

244 **Fig. 8** Comparison of experimental and numerical displacement-time curves of typical joints in  
245 test D-2

246 where  $\Lambda(0)$  and  $\Lambda(t)$  are the elasto-plastic buckling capacity of AARS with gusset joints  
247 at times 0 and  $t$  of the fire process, respectively. Note that  $\Lambda(0)$ , i.e., the room-

248 temperature buckling capacity, can be calculated based on the formulae proposed in  
 249 reference [20] or the room-temperature numerical model introduced in Section 2.1,  
 250 while  $\Lambda(t)$  should be determined based on the numerical model proposed in Section 2.2.



255 **Fig. 9** Comparison of experimental and numerical deformation patterns

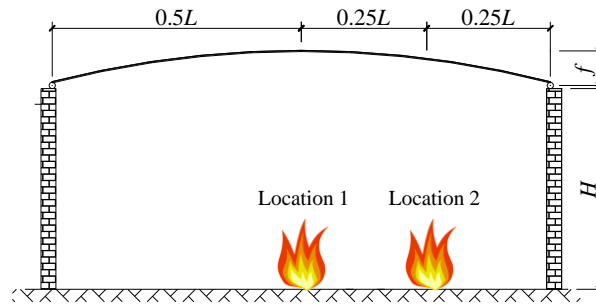
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### 257 3.1 Analysis scheme

258 In order to explore the calculation method of  $k_{\Lambda}(t)$  (abbreviated as  $k_{\Lambda}$  hereinafter) under  
 259 common fire conditions, numerical models are established based on the following  
 260 analysis scheme:

- 261 (1) Span  $L$ : 25, 30, 40 m;  
 262 (2) Height-to-span ratio  $f/L$ : 1/3, 1/4, 1/5;  
 263 (3) Number of rings: 10, 12, 14;  
 264 (4) Cross-section: H250×200×8×10, H300×200×10×14, and H400×250×10×16;  
 265 (5) Support conditions: pinned support, fixed support at the periphery;  
 266 (6) Fire power  $Q$ : 2, 8, 25 MW;  
 267 (7) Height of the supporting structure  $H$ : 0, 5, 10 m;  
 268 (8) Fire location: at the center (location 1), at the corner (location 2).

269 Note that items (1), (2), (3), and (5) are determined according to the engineering  
 270 experience, while the cross-section of the members, i.e., item (4), is determined based  
 271 on the principle of avoiding the in-plane buckling of the member [27] and local buckling  
 272 of the cross-section [28]. Identical cross-sections are assigned for all the members  
 273 because the gusset joint requires the height of the H-shaped members to be exactly the  
 274 same. Illustrations of some parameters are shown in Fig. 10.



275  
 276 **Fig. 10** Numerical model parameters

277 According to the heat release rate-time curves of ordinary large-space fire  
 278 combustibles given in the NFPA handbook [29], the fire duration will not exceed 2000  
 279 s. In order to study the variation trend of the elasto-plastic ultimate bearing capacity of  
 280 AARSs under the whole fire process, the fire duration  $t_{max}$  is selected as 2400 s, and the  
 281 interval of the evaluation of the ultimate bearing capacity is 240 s, considering both the  
 282 accuracy and the computational cost.

283 The empirical formula proposed by Du and Li [13] without the drop in the  
 284 temperature is used to calculate the air temperature field as suggested by reference [9].  
 285 The temperature development of aluminum alloy structural components is calculated  
 286 according to the point assumption-based method proposed in reference [14].

287 The 6061-T6 aluminum alloy is selected as the material of the numerical model.  
 288 Its material properties at room and elevated temperatures are determined according to  
 289 the Eurocode [24].

290

### 291 **3.2 Influence of number of element divisions**

292 Member buckling directly influences the global stability of reticulated shells [30],  
 293 which can be simulated by simulating a member with multiple elements [31]. However,  
 294 increasing the number of element divisions greatly affects the total number of nodes  
 295 and elements in the numerical model, resulting in a higher computational cost.  
 296 Therefore, this section investigates the influence of the number of element divisions on  
 297 the reduction factor  $k_{\Lambda}$ .

298 Fig. 11 shows the  $k_{\Lambda}$ - $t$  curves of the two fire locations when different numbers of  
 299 segments are used to simulate the member, respectively. The span of the numerical

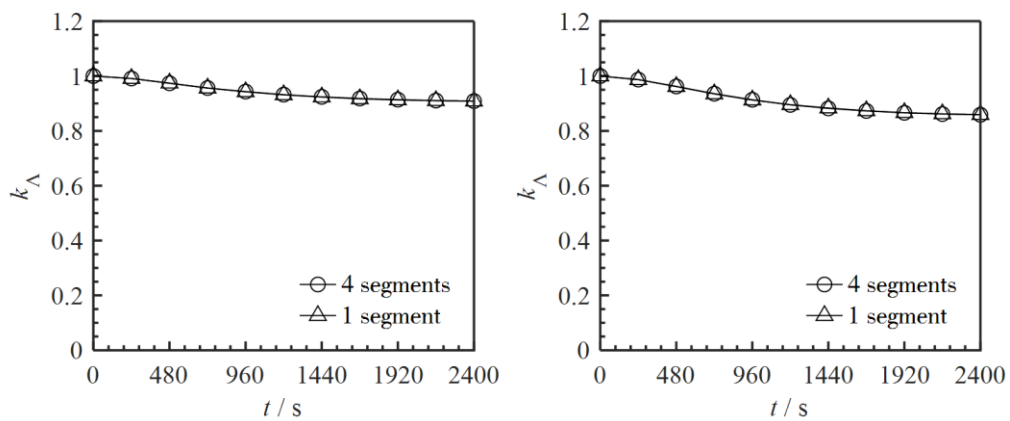
300 model is 40 m, the height-to-span ratio is 1/3, the cross-section is H400×250×10×16,  
 301 the number of rings is 12, the support condition is pinned support, the height of the  
 302 supporting structure is 0 m, and the fire power is 8 MW. It can be seen that the  $k_{\Lambda}$ - $t$   
 303 curves are coincident when the number of element divisions increases from 1 to 4,  
 304 indicating that  $k_{\Lambda}$  is independent of the number of element divisions. Note that the  
 305 parameters not specifically described in the following sections are the same as those  
 306 mentioned above.

307 This is because the cross-sections are designed to prevent member buckling and  
 308 local buckling, as discussed in Section 3.1. Therefore, there will be no interaction  
 309 between member buckling and global buckling in the numerical examples. To reduce  
 310 the computational cost, only one element will be used to simulate the member in the  
 311 following numerical analysis. Meanwhile, the shape function of the element adopts  
 312 cubic polynomial to ensure accuracy.

313

### 314 3.3 Influence of span

315 When the height-to-span ratio and the span-to-thickness ratio, i.e., the ratio of the span  
 316 to the height of the member, are constant, the span influences the distribution of the air  
 317 temperature field. Fig. 12 shows the  $k_{\Lambda}$ - $t$  curves of the two fire locations with different  
 318 spans, i.e., 25, 30, and 40 m.



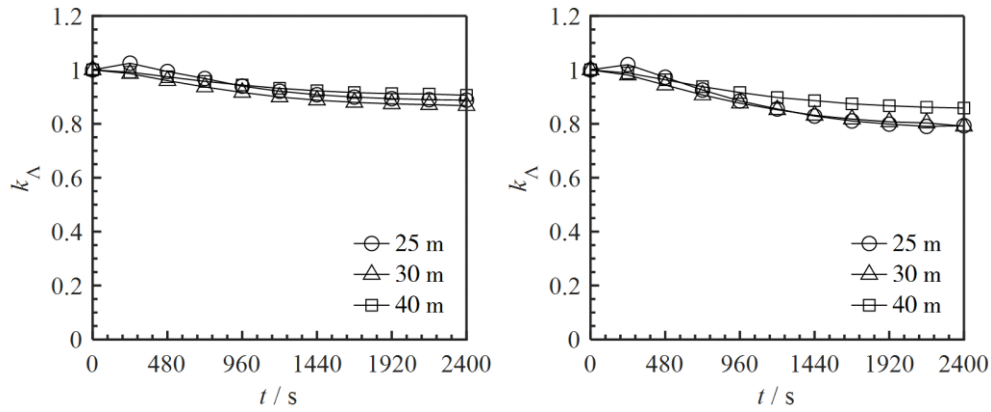
319

320 (a) Fire location 1

(b) Fire location 2

321

**Fig. 11** Influence of number of element divisions on  $k_{\Lambda}$



(a) Fire location 1

(b) Fire location 2

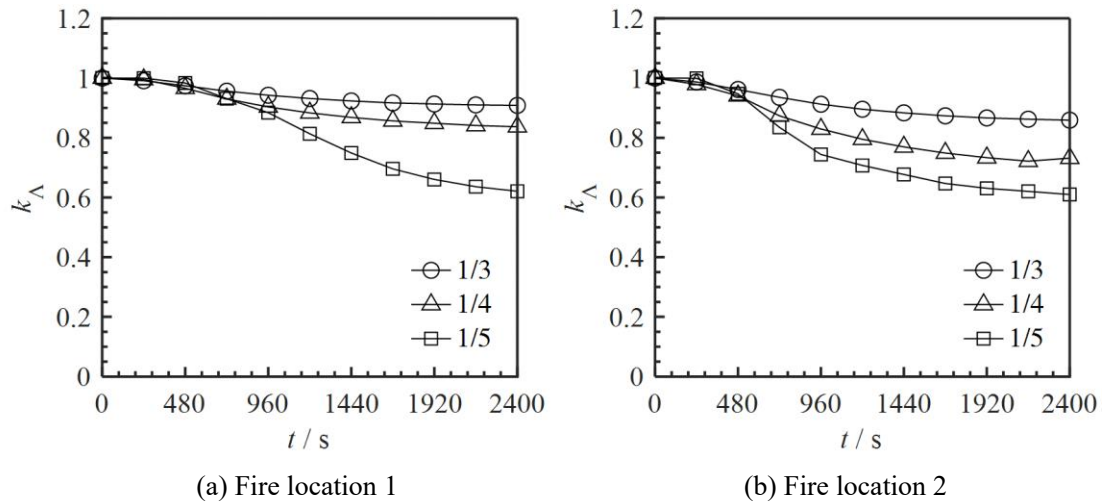
**Fig. 12** Influence of span on  $k_{\Lambda}$

The following conclusions can be obtained from Fig. 12:

- (1) When the span is 25 m,  $k_{\Lambda}$  increases at the initial stage of the fire process, while the value of  $k_{\Lambda}$  monotonically decreases with the time when the span is 30 m or 40 m. This is because the air temperature field and the thermal expansion are more uniformly distributed when the span is smaller. As the maximum temperature of structural components is relatively small at the initial stage of the fire process, the reduction in the material properties is not significant. At this time, the thermal expansion can be regarded as a minor variation in the structural shape, which can result in an increase in the ultimate bearing capacity [32];
- (2) When the fire location moves from the center to the corner,  $k_{\Lambda}$  greatly decreases at the late stage of the fire process, while the reduction in  $k_{\Lambda}$  becomes less significant with the increase of the span. This is because the asymmetric air temperature field induced by the fire at the corner is more disadvantageous than the symmetric air temperature field induced by the fire at the center, and the extra compressive forces due to the ferrule effect become more severe.

### 3.4 Influence of height-to-span ratio

The shape of spherical AARSs is determined by the height-to-span ratio, which also affects the global stability [20] and the air temperature field. Fig. 13 shows the  $k_{\Lambda}$ - $t$  curves of the two fire locations under various height-to-span ratios, i.e., 1/3, 1/4, and 1/5.



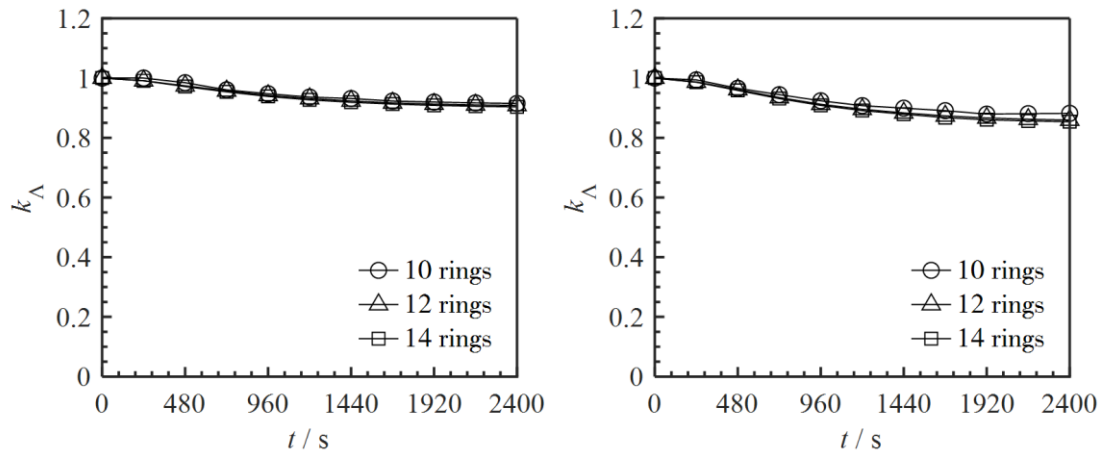
**Fig. 13** Influence of height-to-span ratios on  $k_{\Delta}$

The following conclusions can be obtained from Fig. 13:

- (1) With the decrease of the height-to-span ratio,  $k_{\Delta}$  gradually decreases simultaneously within the fire process. Therefore, the reduction in the ultimate bearing capacity of AARSs with small height-to-span ratios is more severe under fire conditions. This is because the compressive forces induced by the ferrule effect are more unfavorable to AARSs with small height-to-span ratios. In specific, AARSs with small height-to-span ratios bear more external load through their bending stiffness instead of the membrane stiffness, so that they are more sensitive to the extra compressive forces, which result in a reduction in the bending stiffness [27]; in addition, as the top joint is closer to the fire source, the average temperature of structural components is higher, and the degradation in material properties is more dramatic;
- (2) When the fire source moves from the center to the corner,  $k_{\Delta}$  of AARSs with various height-to-span ratios all decrease, and the maximum decline occurs when the height-to-span ratio is 1/4. This is because when the fire source is located at the center, the favorable effect of the symmetric thermal expansion [9] can neutralize the reduction in the ultimate bearing capacity.

### 3.5 Influence of number of rings

The ultimate bearing capacity of K6 AARSs improves with the increase of the number of rings at room temperature [20]. Fig. 14 shows the  $k_{\Delta}$ - $t$  curves of the two fire locations under various numbers of rings, i.e., 10, 12, and 14. Note that the cross-section considered in this section is H300×200×10×14. It can be seen from Fig. 14 that the effect of the number of rings on  $k_{\Delta}$  is not significant.

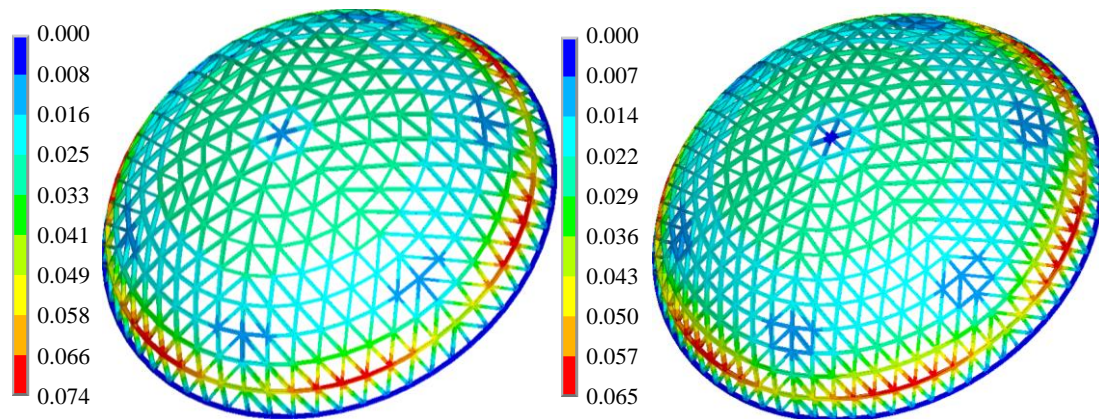


(a) Fire location 1

(b) Fire location 2

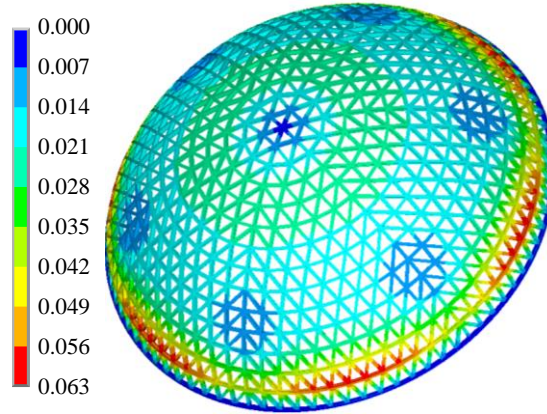
**Fig. 14** Influence of number of rings on  $k_{\Lambda}$

In order to explore the mechanism, Fig. 15 shows the ultimate states of the AARSs with different numbers of rings at  $t = 2400$  s when the fire is located at the center. It can be observed that the shells share the same failure mechanism, which is excessive bulge deformation at the outmost ring. Notably, this failure mechanism is in accordance with the analysis by Zhu *et al.* [10], that the compressive forces of members at the outmost ring are the highest among all members due to the ferrule effect. In specific, although the ultimate bearing capacity of AARSs at room temperature can be increased by increasing the number of rings [20], the relative stiffness of the outmost ring almost remains unvaried, resulting in identical values of  $k_{\Lambda}$ . As a result, the number of rings will be taken as a constant value when deriving the formula of  $k_{\Lambda}$  in Section 4.



(a) 10 rings

(b) 12 rings

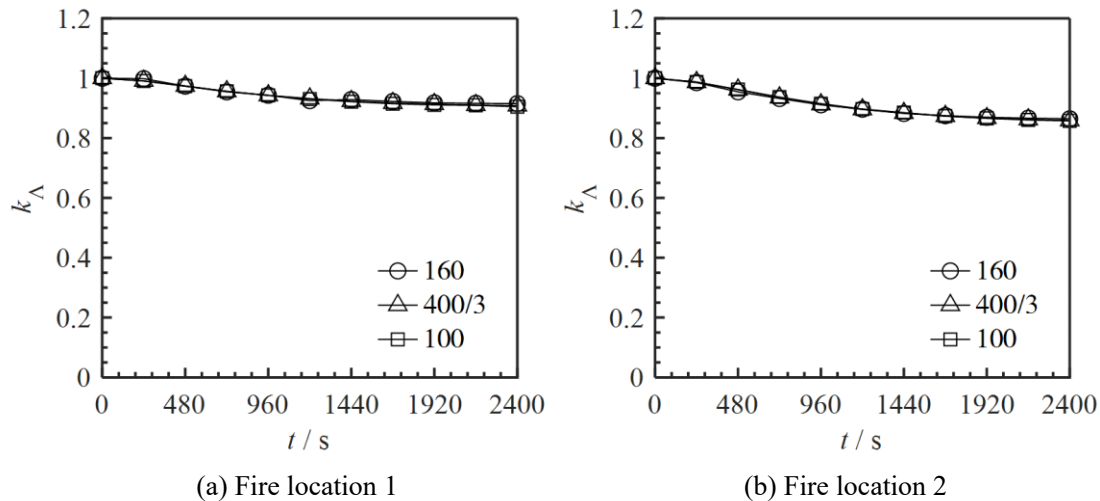


(c) 14 rings

**Fig. 15** Ultimate states of AARSs with different numbers of rings at  $t = 2400$  s (fire located at the center, unit: m)

### 3.6 Influence of span-to-thickness ratio

When the span is constant, the ultimate bearing capacity of a K6 AARS at room temperature increases with the decrease of the span-to-thickness ratio [20]. Fig. 16 shows the  $k_{\Lambda}$ - $t$  curves of the two fire locations under different span-to-thickness ratios, i.e., 160, 300/4, and 100. As the span of the numerical model is 40 m, the corresponding cross-sections of the members are H250×200×8×10, H300×200×10×14, and H400×250×10×16, respectively.

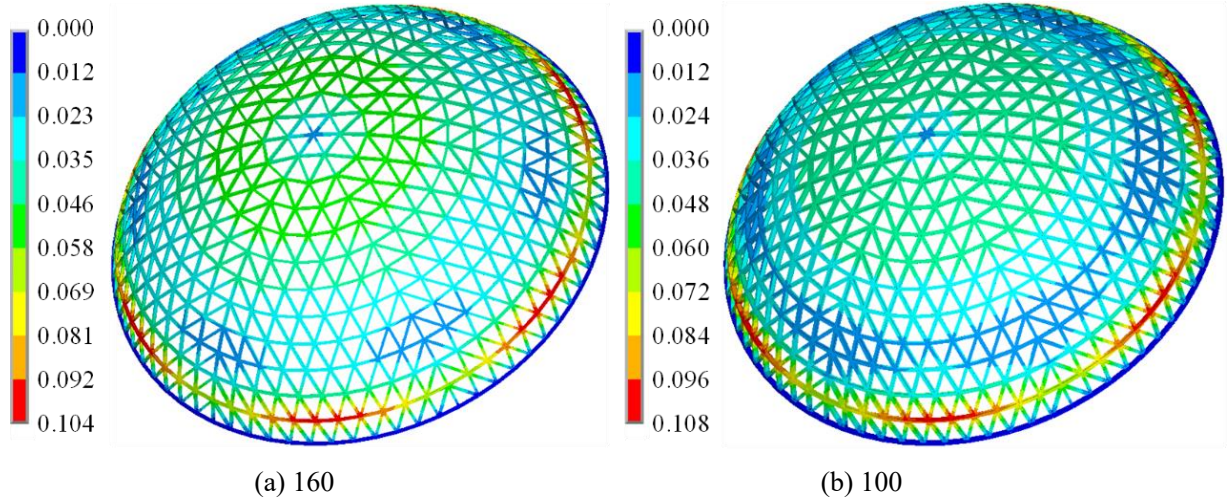


**Fig. 16** Influence of span-to-thickness ratios on  $k_{\Lambda}$

It can be seen from Fig. 16 that the  $k_{\Lambda}$ - $t$  curves are almost coincident. Fig. 17 shows the ultimate states of the AARSs with different span-to-thickness ratios at  $t = 2400$  s when the fire is located at the center. Notably, the ultimate state of the AARS with the span-to-thickness ratio of 400/3 is the same as in Fig. 15(b). The mechanism is almost the same as described in Section 3.5. Since member buckling has already been avoided,



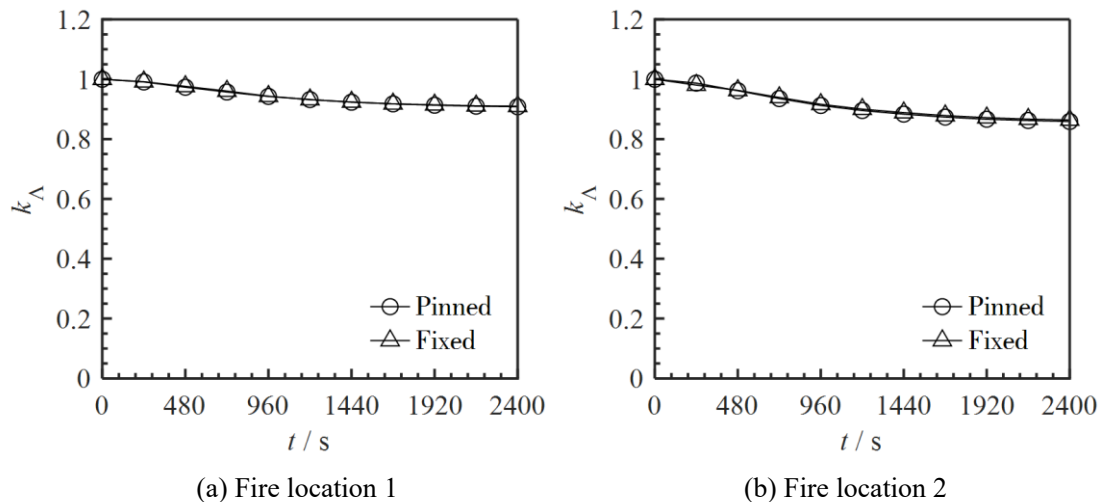
409 although enlarging the cross-section of the member leads to an increase in the global  
 410 stiffness, the relative stiffness of the outmost ring is not changed. Therefore, the values  
 411 of  $k_{\Lambda}$  remain unvaried. In this way, the span-to-thickness ratio will be taken as a constant  
 412 value when deriving the formula of  $k_{\Lambda}$  in Section 4.



**Fig. 17** Ultimate states of AARSs with different span-to-thickness ratios at  $t = 2400$  s (fire located at the center, unit: m)

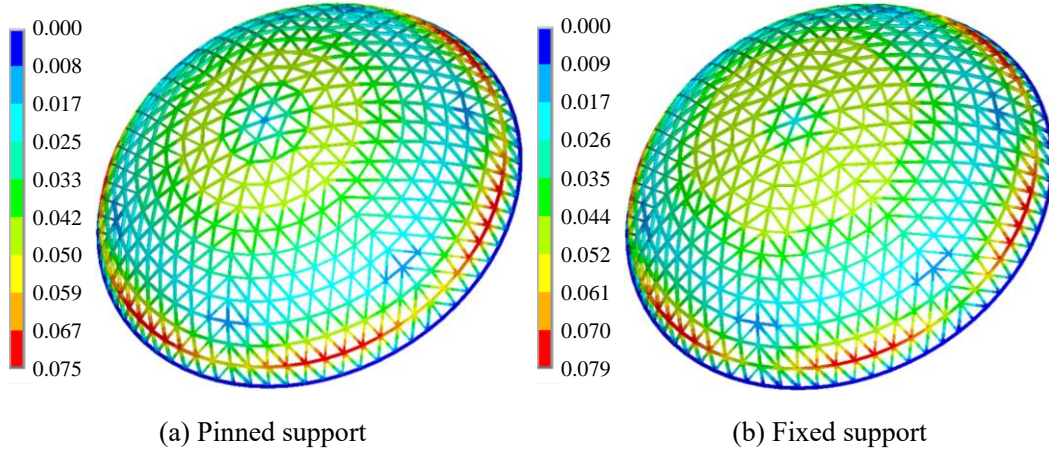
### 3.7 Influence of support condition

418 The support condition is influential to the room-temperature elasto-plastic buckling  
 419 capacity of AARSs as there is an approximate 10% reduction in the buckling capacity  
 420 when the support condition varies from fixed support to pinned support [20]. Fig. 18  
 421 shows the  $k_{\Lambda}$ - $t$  curves of the two fire locations under different support conditions, i.e.,  
 422 pinned and fixed support. Note that the cross-section considered in this section is  
 423 H250×200×8×10. It can be observed from Fig. 18 that the influence of support  
 424 conditions on  $k_{\Lambda}$  is not significant.  
 425



**Fig. 18** Influence of support conditions on  $k_{\Lambda}$

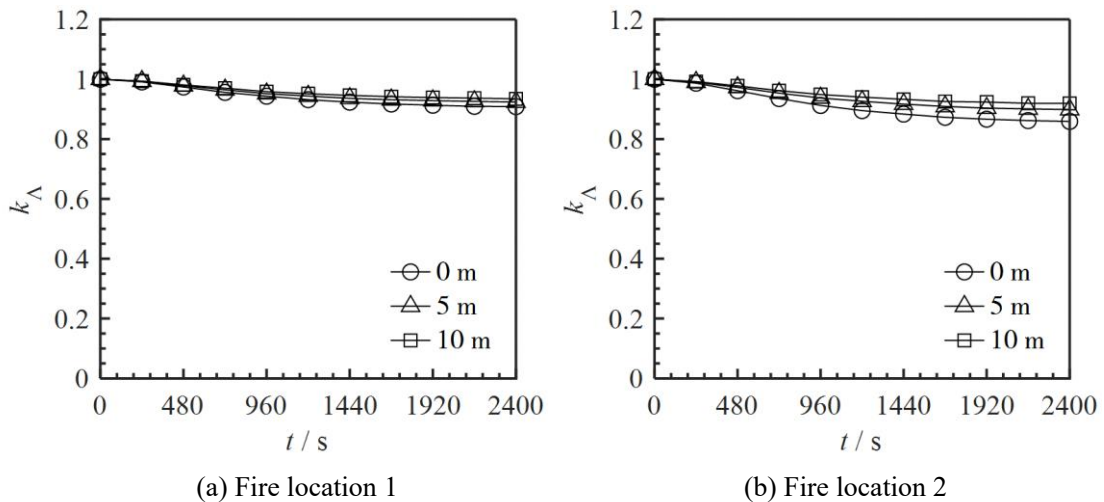
429 Fig. 19 shows the ultimate states of the AARSs with different support conditions at  
 430  $t = 2400$  s when the fire is located at the center. It can be observed that the failure mode  
 431 remains the same when the support conditions are different, i.e., the relative stiffness of  
 432 the outmost ring is not changed by the support condition. Therefore, in the subsequent  
 433 numerical analysis, only the pinned-supported AARSs will be analyzed in order to  
 434 reduce the computational cost.



435  
 436 (a) Pinned support (b) Fixed support  
 437 **Fig. 19** Ultimate states of AARSs with different support conditions at  $t = 2400$  s (fire located at the  
 438 center, unit: m)

### 439 3.8 Influence of height of supporting structure

440 The height of the supporting structure directly impacts the air temperature field. Fig. 20  
 441 shows the  $k_{\Lambda}$ - $t$  curves of the two fire locations under different heights of the supporting  
 442 structure, i.e., 0 m, 5 m, and 10 m. Note that the cross-section considered in this section  
 443 is H300×200×10×14.



444  
 445 (a) Fire location 1 (b) Fire location 2  
 446 **Fig. 20** Influence of height of supporting structure on  $k_{\Lambda}$

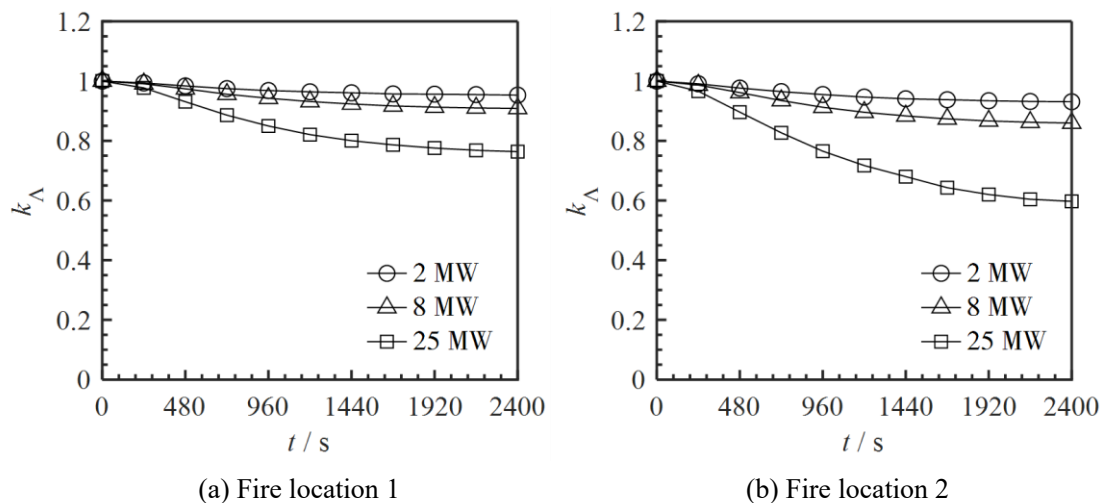
447 The following conclusions can be obtained from Fig. 20:

- 448 (1) With the increase of the height of the supporting structure,  $k_{\Lambda}$  increases at each

449 time within the fire process. This is because the height of the supporting  
 450 structure can also be regarded as the minimum distance between the fire source  
 451 and the structural components. Hence, the air temperature near the structural  
 452 components and the radiative heat flux from the fire source decrease [14]. As  
 453 a result, the degradation in material properties, as well as the thermal  
 454 compressive force induced by the ferrule effect, becomes less severe;  
 455 (2) With the increase in the height of the supporting structure, the increase rate of  
 456  $k_{\Lambda}$  is reduced. Therefore, the economic benefit of considerably adjusting the  
 457 structural layout for ensuring fire safety is low for large-space structures.  
 458

### 459 3.9 Influence of fire power

460 The fire power directly affects the maximum temperature of the air temperature field  
 461 [9]. Fig. 21 shows the  $k_{\Lambda}$ - $t$  curves of the two fire locations under different fire powers,  
 462 i.e., 2 MW, 8 MW, and 25 MW. Note that the cross-section considered in this section  
 463 is H300×200×10×14.



464  
 465 (a) Fire location 1 (b) Fire location 2  
 466 **Fig. 21** Influence of fire power on  $k_{\Lambda}$

467 It can be concluded from Fig. 21 that with the increase of the fire power,  $k_{\Lambda}$   
 468 decreases at each time of the fire process. This is due to the increase in the temperature  
 469 at each height of the fire centerline and the radiative heat flux with the increase of the  
 470 fire power. Therefore, the reduction in material properties and extra compressive forces  
 471 caused by the high temperature becomes more significant, resulting in a more severe  
 472 reduction in the ultimate bearing capacity.  
 473

### 474 4 Practical design formula

475 In the initial/concept design stage, it is necessary to predict the ultimate bearing capacity  
 476 of AARSs under fire conditions. In this section, a practical design formula of the

477 reduction coefficient  $k_{\Lambda}$  will be derived based on further parametric analysis.

478

#### 479 4.1 Form of formula

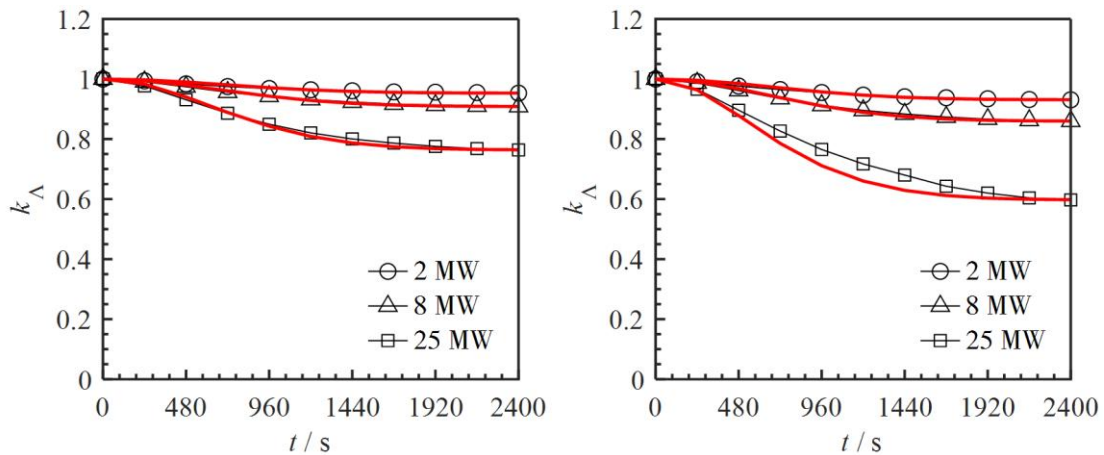
480 The following rules can be obtained by observing the  $k_{\Lambda}$ - $t$  curves in Sections 3.2 to 3.9:

- 481 (1) The value of  $k_{\Lambda}$  is 1.0 at 0 s as the fire has not affected the structure, i.e.,  $k_{\Lambda}(0)$   
482 = 1.0;
- 483 (2) The value of  $k_{\Lambda}$  almost decreases monotonously with time and reaches the  
484 minimum value  $k_{\Lambda,\min}$  at the end of the fire process, i.e.,  $k_{\Lambda}(2400) = k_{\Lambda,\min}$ ;
- 485 (3) The value of  $k_{\Lambda}$  varies slowly at the early stage of the fire process, rapidly in  
486 the middle stage, and slowly again at the later stage. Hence, the  $k_{\Lambda}$ - $t$  curve  
487 should include two inflection points.

488 Thus, the calculation formula of  $k_{\Lambda}(t)$  can be constructed as

$$489 k_{\Lambda}(t) = \frac{k_{\Lambda,\min}}{1 + (k_{\Lambda,\min} - 1)e^{-10^{-6}t^2}} \quad (3)$$

490 where  $t$  is the time (s) ranging in  $0 \leq t \leq 2400$ . It can be seen from Eq. (3) that the  
491 formula of  $k_{\Lambda}(t)$  only contains one undetermined parameter  $k_{\Lambda,\min}$ . Take the curves of  
492 the fire power series in Section 3.9 as the example, and Fig. 22 shows the comparison  
493 between the numerical curve and the curve calculated by Eq. (3), when  $k_{\Lambda,\min}$  is directly  
494 taken as the accurate result of the numerical curve. In Fig. 22, the solid red line  
495 represents the curve of Eq. (3). It can be seen that the form of Eq. (3) can accurately  
496 predict the variation of the reduction factor of the ultimate bearing capacity in the whole  
497 process of the fire. Thus, the equation of  $k_{\Lambda}(t)$  can be determined based on two thermal-  
498 structural coupled elasto-plastic analyses, i.e., the calculation of  $k_{\Lambda,\min}$ .



499

500 (a) Fire location 1

500 (b) Fire location 2

501

501 **Fig. 22** Comparison of numerical curves and the curve of the proposed formula

502

## 503 4.2 Parametric analysis scheme

504 In order to further reduce the computational cost in practical engineering applications,  
505 the practical calculation method of  $k_{\Lambda, \min}$  under common fire scenarios is expected to  
506 be proposed.

507 According to the parametric analysis in Sections 3.2 to 3.9, the value of  $k_{\Lambda}$  should  
508 be only related to the span, the height-to-span ratio, the height of the supporting  
509 structure, the fire power, and the fire location. As other parameters are kept constant,  
510 i.e., the number of rings is 12, the span-to-thickness ratio is 100, and the support  
511 condition is pinned support, the numerical models of 162 reticulated shells are  
512 established considering the following parameters:

- 513 (1) Span  $L$ : 25, 30, 40 m;
- 514 (2) Height-to-span ratio  $f/L$ : 1/3, 1/4, 1/5;
- 515 (3) Fire power  $Q$ : 2, 8, 25 MW;
- 516 (4) Height of supporting structure  $H$ : 0, 5, 10 m;
- 517 (5) Fire location: at the center (location 1), at the corner (location 2).

## 518 4.3 Regression based on machine learning

519 As indicated in Section 4.1,  $\Lambda(0)$  and  $\Lambda(2400)$  will be calculated in order to determine  
520 the value of  $k_{\Lambda, \min}$  for each numerical model:

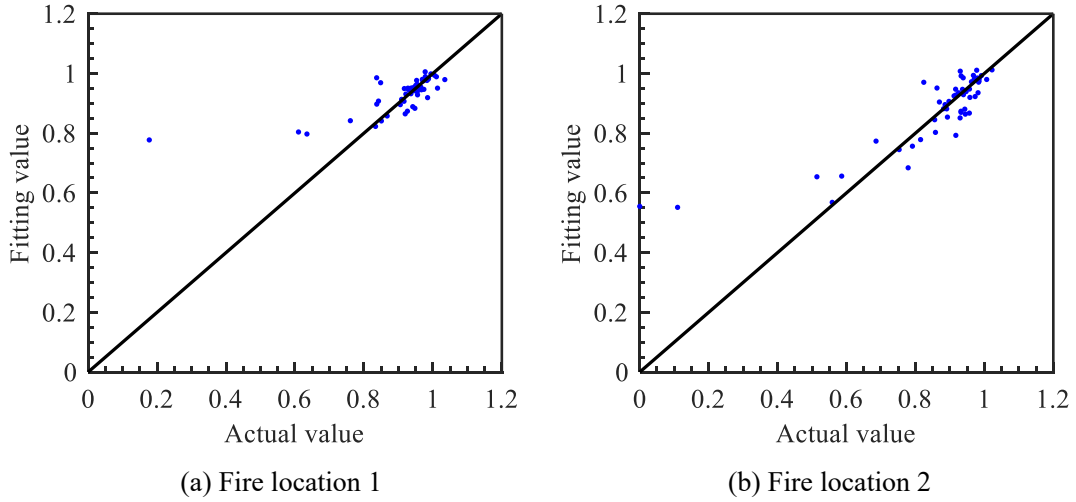
$$521 \quad k_{\Lambda, \min} = \frac{\Lambda(2400)}{\Lambda(0)} \quad (4)$$

522 On this basis, using the Statistics and Machine Learning Toolbox in MATLAB  
523 R2020a [33], the support vector machine with a linear kernel function is used to fit the  
524 numerical results, while quadratic terms are introduced to improve the accuracy (see  
525 literature [31] for specific principles). Hence,  $k_{\Lambda, \min}$  can be calculated as follows:

$$526 \quad k_{\Lambda, \min} = p_1 L + p_2 (f/L) + p_3 Q + p_4 H + p_{1,1} L^2 + p_{1,2} L \cdot (f/L) + p_{1,3} L \cdot Q + p_{1,4} L \cdot H \quad (5) \\ + p_{2,2} (f/L)^2 + p_{2,3} (f/L) \cdot Q + p_{2,4} (f/L) \cdot H + p_{3,3} Q^2 + p_{3,4} Q \cdot H + p_{4,4} H^2 + b$$

527 where  $p_i$  is the coefficient of the  $i$ th ( $1 \leq i \leq 4$ ) linear term,  $p_{i,j}$  is the coefficient of the  
528  $ij$ th ( $i \leq j \leq 4$ ) quadratic term, and  $b$  is the undetermined bias. For the two fire locations,  
529 the fitting values of each parameter in Eq. (5) are shown in Table 1. Denote the result  
530 calculated by Eq. (5) as the fitting value and the results calculated by the thermal-  
531 structural coupled analysis as the actual value. Fig. 23 shows the comparison of the  
532 fitting value and the actual value. It can be seen that the error is relatively small, and it  
533 is reasonable to use Eqs. (3) and (5), together with Table 1, to rapidly predict the  
534 ultimate bearing capacity at the initial stage of the design of AARSs. This way,

535 repetitive thermal-structural coupled analyses under fire conditions can be avoided at  
 536 the initial/concept design stage. However, it is worth noting that Eqs. (3) and (5) are  
 537 only applicable to K6 AARSs when the span is 25 ~ 40 m, the height-to-span ratio is  
 538 1/5 ~ 1/3, the height of the supporting structure is 0 ~ 10 m, and the fire power is 2 ~ 8  
 539 MW.



540  
 541 (a) Fire location 1 (b) Fire location 2  
 542 **Fig. 23** Comparison between the fitting value of  $k_{\Lambda, \min}$  and actual values

543 **Table 1** Fitting parameters of  $k_{\Lambda, \min}$  under common fire scenarios

Parameter	Location 1	Location 2
$p_1$	0.0534	0.3961
$p_2$	0.0205	-0.1703
$p_3$	-0.1550	-0.2748
$p_4$	0.2631	0.5988
$p_{1,1}$	-0.0459	-0.4569
$p_{1,2}$	-0.0273	0.1229
$p_{1,3}$	0.1311	0.3200
$p_{1,4}$	-0.1181	-0.3942
$p_{2,2}$	0.0303	0.1485
$p_{2,3}$	0.0521	-0.0552
$p_{2,4}$	-0.1272	-0.1364
$p_{3,3}$	-0.1550	-0.2748
$p_{3,4}$	0.1044	0.2726
$p_{4,4}$	-0.0442	-0.1622
$b$	0.9313	0.8820

544 Here we need to note that the machine learning techniques are used since the  
 545 reduction factors of the ultimate bearing capacity of K6 AARSs are highly non-linear  
 546 with respect to the parameters specified in Eq. (5). In this way, traditional curve-fitting

547 techniques, although applicable, will provide complex fitting formulae. An example can  
548 be referred to in literature [20]. Besides, we aim to provide an explicit formula instead  
549 of a black box to better serve practical engineering. Therefore, we have chosen the  
550 support vector machine with a linear kernel function rather than a Gaussian kernel  
551 function or the neural networks to establish the machine learning model, though they  
552 may have a better regression performance.

553 However, there are still a few outliers in Fig. 23. Although this also indicates that  
554 overfitting does not exist in our trained model, we still need to emphasize that the  
555 thermal-structural coupled analysis should be conducted after determining the structural  
556 design scheme in the initial/concept design stage if the requirements proposed in  
557 Section 5.1 (for ignoring the ultimate bearing capacity analysis) are not satisfied.

558

## 559 **5 Practical design suggestions**

560 Besides the formula of the ultimate bearing capacity, practical design suggestions,  
561 including conditions of ignoring the ultimate bearing capacity analysis of K6 AARs,  
562 and conditions of ignoring the radiative heat flux, are proposed in this section, aiming  
563 to reduce the computational cost of the field simulation and the thermal-structural  
564 coupled analysis.

565

### 566 **5.1 Conditions of ignoring the ultimate bearing capacity analysis of K6 AARs**

567 The analysis results in Sections 3.8 and 3.9 show that the reduction in the ultimate  
568 bearing capacity under fire becomes less significant with the decrease of  $Q$  and the  
569 increase of  $H$ . Therefore, there should be a critical combination of  $Q$  and  $H$  that makes  
570 the reduction of the ultimate bearing capacity negligible. In order to explore the critical  
571 combination to simplify the calculation process, this section conducts further numerical  
572 analysis with respect to the influential parameters. Unvaried parameters include the  
573 span (40 m), number of rings (12), cross-section (H300×200×10×14), and support  
574 condition (pinned support). Influential parameters are varied according to the following  
575 scheme:

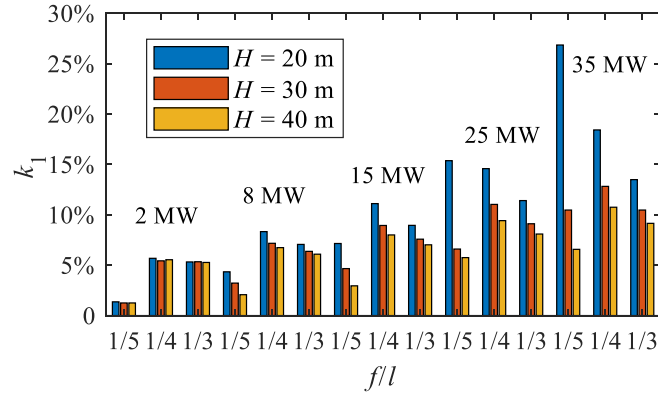
- 576 (1) Height-to-span ratio  $f/L$ : 1/3, 1/4, 1/5;  
577 (2) Fire power  $Q$ : 2, 8, 15, 25, 35 MW;  
578 (3) Height of supporting structure  $H$ : 20, 30, 40 m;  
579 (4) Fire location: at the center (location 1), at the corner (location 2).

580 Note that the fire duration is also conservatively taken as 2400 s.

581 Denote  $k_i$  ( $i = 1, 2$ ) as the minimum reduction factor of the ultimate bearing capacity  
582 of the whole fire process at the  $i$ th fire source position:

583

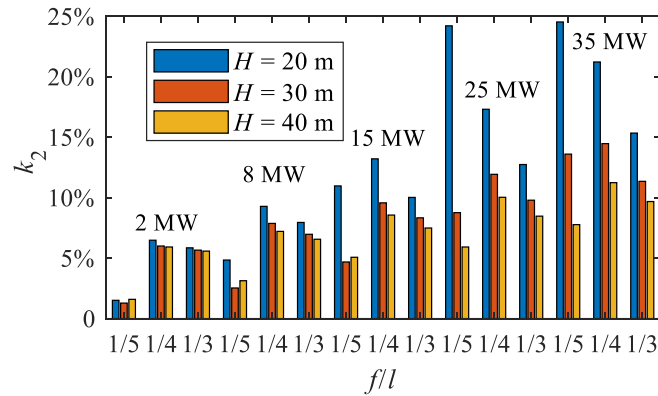
$$k_i = 1 - \frac{\Lambda_i(2400)}{\Lambda(0)} \quad (6)$$



584

585

(a) Fire location 1



586

587

588

(b) Fire location 2

**Fig. 24** Results of  $k_i$

589

590

The values of  $k_i$  values from the numerical analysis are summarized in Fig. 24, and the following design suggestions can be drawn:

591

592

593

594

595

596

597

598

599

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601

602

- (1) If the designer can accept a reduction of the ultimate bearing capacity within 5 %, then when  $f/L$  equals 1/5,  $Q$  is less than or equal to 8 MW, and the minimum distance between the fire source and the structure is greater than 20 m, the ultimate bearing capacity analysis under fire can be ignored;
- (2) If the designer can accept a reduction of ultimate bearing capacity within 10 %, the ultimate bearing capacity analysis under fire can be ignored when the  $f/L$  equals 1/3 or 1/5, the fire power is less than or equal to 15 MW, and the minimum distance between the fire source and the structure is greater than 20 m; when  $f/L$  is 1/4, the maximum  $Q$  should be limited to 8 MW;
- (3) When  $Q$  is greater than or equal to 25 MW, the ultimate bearing capacity of the structure under fire must be conducted since the reduction in the ultimate bearing capacity is significant.



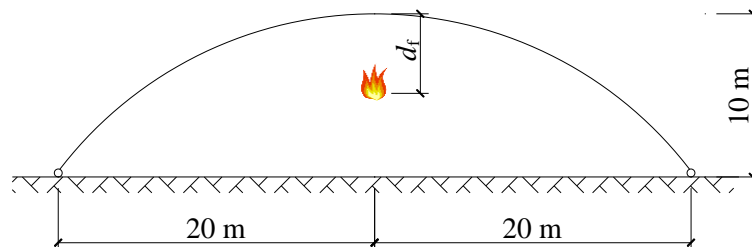
603 **5.2 Conditions of ignoring the radiative heat flux**

604 Zhu *et al.* [14] highlighted that the radiative heat flux plays a more important role in  
605 large-space fires compared to compartment fires, yet the contribution of the radiative  
606 heat flux to the temperature development of structural components decays with the  
607 increase of the distance between the structural component and the fire source. Therefore,  
608 this section explores the critical condition that the radiative heat flux can be ignored to  
609 provide suggestions for architectural composition and simplification of calculation. The  
610 basic model is the same as described in Section 5.1, whereas  $f/L$  and  $H$  are fixed as 1/4  
611 and 0, respectively. Influential parameters are varied based on the following scheme:

- 612 (1) Fire power  $Q$ : 2, 8, 25 MW;
- 613 (2) Radiation heat flux: considered, ignored;
- 614 (3) Fire source-structural component distance  $d_f$ : 1, 3, 5, 7 m;
- 615 (4) Fire location: below the roof, near the support.

616 The fire source-structural component distance  $d_f$  refers to the distance between the  
617 centroid of the fire source and the structural components. Definitions of the fire location  
618 and  $d_f$  are shown in Fig. 25.

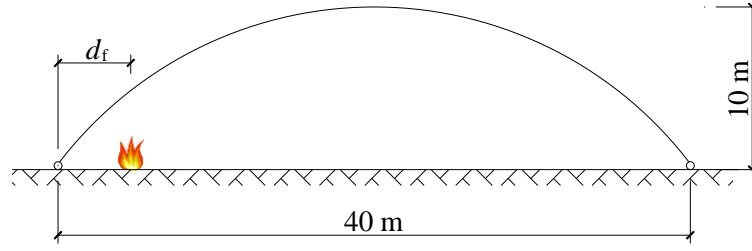
619 Since the fire source is very close to the structure, the empirical formula in  
620 reference [13] cannot be used to calculate the air temperature field. Hence, the FDS  
621 models are established using the method proposed by Zhu *et al.* [10] to calculate the air  
622 temperature field. Besides, the ultimate fire resistance time of the structure, instead of  
623 the ultimate bearing capacity, is used to evaluate the structural capacity of the structure  
624 under fire, and a uniformly-distributed surface load of 1 kN/m<sup>2</sup> is considered. Here we  
625 note that the fire-resistant time of the structure is defined as the moment when the  
626 stiffness matrix of the structure is singular and no further load can be applied. The fire  
627 duration is also taken as 2400 s.



628

629

(a) Fire under the roof



(b) Fire near the support

**Fig. 25** Definitions of parametric analysis

a) Fire under the roof

The numerical analysis results when the fire is under the roof are shown in Table 2. In Table 2,  $t_r$  and  $t_{nr}$  are the ultimate fire resistance time when the radiative heat flux is considered and ignored, respectively;  $e_t$  and  $e_T$  are the relative errors of the ultimate fire resistance time and the maximum member temperature difference, defined as

$$e_t = \frac{t_{nr} - t_r}{t_r} \times 100\% \quad (7)$$

$$e_T = \max_t \left[ \frac{T_{nr}(t) - T_r(t)}{T_r(t)} \right] \times 100\% \quad (8)$$

where  $T_r(t)$  and  $T_{nr}(t)$  are the member temperature at time  $t$  when the radiative heat flux is considered and ignored, respectively.  $\Delta T_{\max}$  is the maximum member temperature difference in the whole fire process, defined as

$$\Delta T_{\max} = \max_t [T_{nr}(t) - T_r(t)] \quad (9)$$

Notably,  $e_t$  is negative only when  $Q$  is 8 MW and  $d_f$  is 5 m, indicating the ultimate fire resistance time is increased by considering the radiative heat flux. Figs. 26 and 27 plot the member temperature contours at the ultimate state of the structure when  $Q$  is 8 MW, and  $d_f$  is 1 m and 5 m, respectively. It can be seen from Fig. 26 that the peak temperature of the structure increases dramatically. In contrast, the peak temperature only increases slightly in Fig. 27, and the member temperature field is also changed. As the thermal expansion becomes more uniform for the state of Fig. 27(a),  $t_r$  is prolonged to be larger than  $t_{nr}$ . Therefore, in order to ensure the accuracy of structural fire analysis results, the influence of radiative heat flux should be considered when calculating the temperature development of structural components.

Table 2 Parameter analysis results when the fire is under the roof.

$Q$ / MW	$d_f$ / m	$t_r$ / s	$t_{nr}$ / s	$e_t$ / %	$\Delta T_{max}$ / °C	$e_T$ / %
2	1	161	187	16.15	-55	-51.43
2	3	408	408	0.00	-17	-20.53
2	5	2400	2400	0.00	-7	-10.63
2	7	2400	2400	0.00	-4	-6.28
8	1	132	216	63.64	-207	-80.63
8	3	262	350	33.59	-53	-50.70
8	5	410	396	-3.41	-23	-32.19
8	7	432	449	3.94	-13	-21.13
25	1	38	187	392.11	-498	-92.54
25	3	178	305	71.35	-162	-76.04
25	5	394	415	5.33	-71	-59.59
25	7	418	430	2.87	-50	-45.49

657  
658  
659

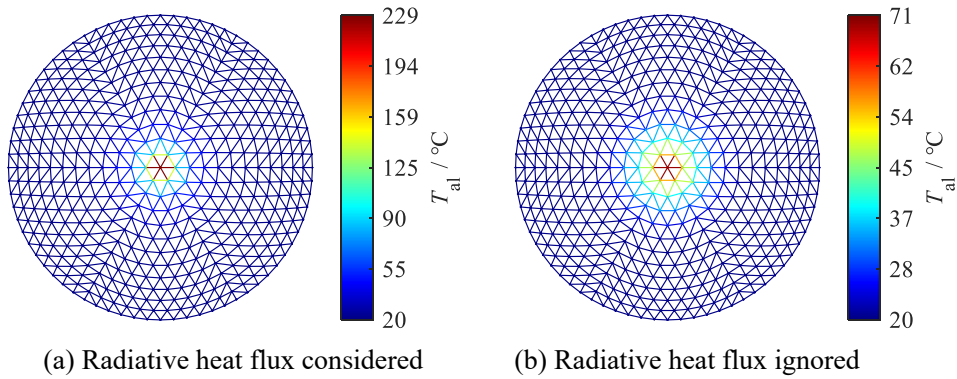


Fig. 26 Member temperature contour of the structure at 132 s ( $Q = 8$  MW and  $d_f = 1$  m)

660  
661  
662

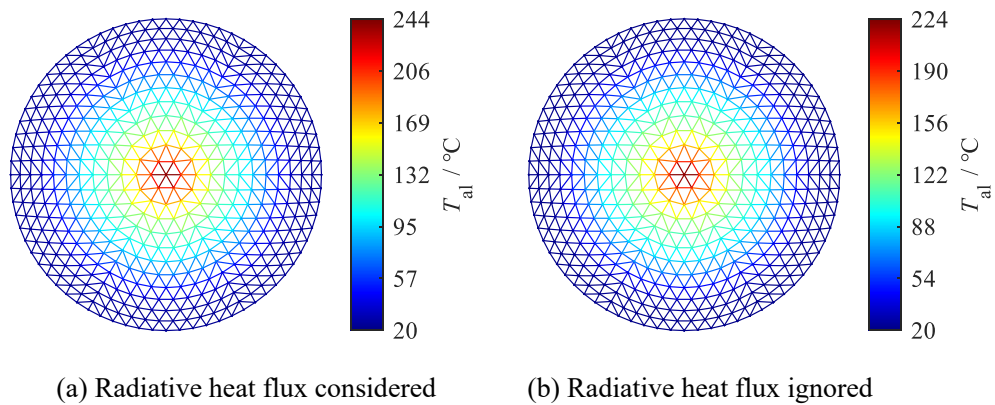


Fig. 27 Member temperature contour of the structure at 396 s ( $Q = 8$  MW and  $d_f = 5$  m)

663 Nonetheless, the relationship of  $t_r \leq t_{nr}$  holds for other situations. Based on the data  
664 in Table 2, it can be concluded that if the designer can accept a maximum of 10 % of  $e_t$ ,  
665 the radiative heat flux (when the fire is under the roof) can be ignored when  $d_f$  is greater  
666 than the critical value  $d_{f,min,r}$ :

667

$$d_{f,\min,r} = \begin{cases} 3 & Q \leq 2 \\ \frac{1}{3}(Q+7) & 2 < Q < 8 \\ 5 & 8 \leq Q \leq 25 \end{cases} \quad (10)$$

668 b) Fire near the support

669 The numerical analysis results when the fire is under the roof are shown in Table  
670 3, where the relationship of  $t_r \leq t_{nr}$  holds for all situations. By comparing Tables 2 and  
671 3, it can be concluded that when the fire is located near the support, the effect of  
672 increasing  $d_f$  on improving the ultimate fire resistance time of the structure is more  
673 significant than that when the fire is below the roof.

674 Similarly, according to the results of Table 3, it can be concluded that if the designer  
675 can accept a maximum of 10 % of  $e_t$ , the radiative heat flux (when the fire is near the  
676 support) can be ignored when  $d_f$  is greater than the critical value  $d_{f,\min,s}$ :

677

Table 3 Parameter analysis results when the fire is near the support

$Q$ / MW	$d_f$ / m	$t_r$ / s	$t_{nr}$ / s	$e_t$ / %	$\Delta T_{\max}$ / °C	$e_T$ / %
2	1	382	2400	528.27	-252	-81.71
2	3	2400	2400	0.00	-38	-52.82
2	5	2400	2400	0.00	-16	-30.97
2	7	2400	2400	0.00	-9	-19.68
8	1	72	2400	3233.33	-504	-94.18
8	3	2400	2400	0.00	-148	-81.54
8	5	2400	2400	0.00	-64	-64.08
8	7	2400	2400	0.00	-35	-49.41
25	1	20	2400	11900.00	-539	-96.36
25	3	252	2400	852.38	-413	-92.87
25	5	1630	2400	47.24	-194	-84.59
25	7	2400	2400	0.00	-109	-75.15

678

$$d_{f,\min,s} = \begin{cases} 3 & Q \leq 8 \\ \frac{1}{17}(4Q+19) & 8 < Q \leq 25 \end{cases} \quad (11)$$

679 When  $d_f$  is small, the adverse effect of the radiative heat flux will significantly  
680 reduce the ultimate fire resistance time of the structure. Therefore, Eqs. (10) and (11)  
681 are suggested to be referred to in order to limit the minimum values of  $d_f$  when  
682 conducting architectural composition to determine the fire scenarios.

683

684 **6 Conclusions**

685 Based on the existing research findings on the high-temperature mechanical  
686 performance of aluminum alloy materials and structural components, this paper  
687 conducts numerical analyses of AARSs under fire conditions considering joint semi-  
688 rigidity. The main contributions or conclusions are as follows:

- 689 (1) The numerical model of AARSs under fire conditions considering joint semi-  
690 rigidity is established and verified against the room-temperature test and the  
691 fire tests. It is notable that the proposed model can also be applied to the  
692 thermal-structural coupled analysis of other structures with semi-rigid joints;
- 693 (2) The reduction factor of the ultimate bearing capacity of K6 AARSs under  
694 common fire conditions is related to the span, the height-to-span-ratio  $f/L$ , the  
695 height of the supporting structure, and the fire power  $Q$ , while it is independent  
696 of the number of element divisions, the number of rings, the span-to-thickness  
697 ratio, and the support condition. The main mechanism of this phenomenon is  
698 that the failure of AARSs is highly associated with extra compressive force at  
699 the outmost ring induced by the ferrule effect, and the influential parameters  
700 will affect the relative stiffness of the outmost ring under fire conditions;
- 701 (3) The reduction in the ultimate bearing capacity of K6 AARSs is rapid at the  
702 stable combustion stage of the fire duration and is slow at the initial and decay  
703 stages;
- 704 (4) Practical design formulae are derived by machine learning via 324 thermal-  
705 structural coupled analysis results to serve the initial/concept design of K6  
706 AARSs.
- 707 (5) Conditions of ignoring the ultimate bearing capacity of K6 AARSs are  
708 proposed. Specifically, if the designer can accept a reduction in the ultimate  
709 bearing capacity within 5 %, the conditions are:  $f/L = 1/5$ ,  $Q \leq 8$  MW, and the  
710 minimum distance between the fire source and the structure is greater than 20  
711 m. If the designer can accept a reduction in the ultimate bearing capacity within  
712 10 %, the conditions are  $f/L = 1/3$  or  $1/5$ ,  $Q \leq 15$  MW, and the minimum  
713 distance between the fire source and the structure is greater than 20 m; when  
714  $f/L = 1/4$ , the maximum  $Q$  should be limited to 8 MW;
- 715 (6) Conditions of ignoring the radiative heat flux are proposed by limiting the  
716 minimum value of the distance between the centroid of the fire source and the  
717 structural component  $d_f$ . It is notable that the limit values of  $d_f$  are suggested  
718 to be referred to in order to limit the minimum values of  $d_f$  when conducting  
719 architectural composition to determine the fire scenarios. This conclusion can

720 be referred to when designing AARSs with any structural forms.

721

## 722 **Statements and Declarations**

723 The authors declare that they have no known competing financial interests or personal  
724 relationships that could have appeared to influence the work reported in this paper.

725

## 726 **Data Availability Statement**

727 Some or all data, models, or codes that support the findings of this study are available  
728 from the corresponding author upon reasonable request.

729

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733

## 734 **References**

735 [1] Meacham BJ, Custer RLP. Performance-based fire safety engineering: An  
736 introduction of basic concepts. *J Fire Prot Eng.* 1995; 7(2): 35-53.

737 <https://doi.org/10.1177/104239159500700201>

738 [2] Roy K, Lim JBP, Lau HH, Yong PM, Cliftona GC, Johnston Ross PD, Wrzesien A,  
739 Mei CC. Collapse behaviour of a fire engineering designed single-storey cold-  
740 formed steel building in severe fires. *Thin-Walled Struct.* 2019; 142: 340-357.

741 <https://doi.org/10.1016/j.tws.2019.04.046>

742 [3] Du E. Experimental and theoretical research on the structural behavior of large  
743 space steel structures subjected to natural fires. Nanjing: Southeast University;  
744 2016. (in Chinese)

745 [4] Lou G, Wang C, Jiang J, Jiang Y, Wang L, Li G. Experimental and numerical study  
746 on thermal-structural behavior of steel portal frames in real fires. *Fire Safety J.*  
747 2018; 98: 48-62.

748 <https://doi.org/10.1016/j.firesaf.2018.04.006>

749 [5] Lou G, Wang C, Jiang J, Jiang Y, Wang L, Li G. Fire tests on full-scale steel portal  
750 frames against progressive collapse. *Journal of Constr Steel Res.* 2018; 145: 137-  
751 152.

752 <https://doi.org/10.1016/j.jcsr.2018.02.024>

753 [6] Alos-Moya J, Paya-Zaforteza I, Hospitaler A, Rinaudo P. Valencia bridge fire tests:  
754 Experimental study of a composite bridge under fire. *Journal of Constr Steel Res.*  
755 2017; 138: 538-554.

756 <https://doi.org/10.1016/j.jcsr.2017.08.008>

- 757 [7] Chen C, Zhang D, Zhang W, Shen B. Experimental behaviors of steel staggered-  
758 truss system exposed to fire under lateral force. *Int J Steel Struct*, 2012; 12(1): 59-  
759 70.  
760 <https://doi.org/10.1007/s13296-012-1006-1>
- 761 [8] Liu M, Zhao J, Jin M. An experimental study of the mechanical behavior of steel  
762 planar tubular trusses in a fire. *Journal of Constr Steel Res*. 2010; 66(4): 504-511.  
763 <https://doi.org/10.1016/j.jcsr.2009.11.005>
- 764 [9] Guo X, Zhu S, Jiang S, Zhang C, Chen C. Fire tests on single-layer aluminum alloy  
765 reticulated shells with gusset joints. *Structures*. 2020; 28: 1137-1152.  
766 <https://doi.org/10.1016/j.istruc.2020.09.054>
- 767 [10] Zhu S, Guo X, Jiang S, Zong S, Chen C. Experimental study on the fire-induced  
768 collapse of single-layer aluminum alloy reticulated shells with gusset joints. *J*  
769 *Struct Eng-ASCE*. 2020; 146(12): 04020268.  
770 [https://doi.org/10.1061/\(ASCE\)ST.1943-541X.0002819](https://doi.org/10.1061/(ASCE)ST.1943-541X.0002819)
- 771 [11] Yin L, Ni Z, Fan F, Qiu P, Kan Q, Ouyang Y. Temperature field characteristics of  
772 cylindrical aluminum alloy reticulated roof system under localized fire. *Fire Safety*  
773 *J*. 2021; 121: 103267.  
774 <https://doi.org/10.1016/j.firesaf.2020.103267>
- 775 [12] Yin L, Ni Z, Fan F, Ye J. Current status analysis of fire protection design system of  
776 long-span spatial structures. *Fire Sci Technol*. 2018; 37: 1178-1180. (in Chinese)
- 777 [13] Du Y, Li G. A new temperature-time curve for fire-resistance analysis of structures.  
778 *Fire Safety J*. 2012, 54: 113-120.  
779 <https://doi.org/10.1016/j.firesaf.2012.07.004>
- 780 [14] Zhu S, Guo X, Tang W, Gao S, Chen C. Temperature development of aluminum  
781 alloy members considering fire radiation. *J Build Eng*. 2021; 42: 102836.  
782 <https://doi.org/10.1016/j.jobe.2021.102836>
- 783 [15] Guo X, Xiong Z, Luo Y, Qiu L, Liu J. Experimental investigation on the semi-rigid  
784 behaviour of aluminium alloy gusset joints. *Thin-Walled Struct*. 2015; 87: 30-40.  
785 <https://doi.org/10.1016/j.tws.2014.11.001>
- 786 [16] Xiong Z, Guo X, Luo Y, Xu H. Numerical analysis of aluminium alloy gusset joints  
787 subjected to bending moment and axial force. *Eng Struct*, 2017; 152: 1-13.  
788 <https://doi.org/10.1016/j.engstruct.2017.09.005>
- 789 [17] Zhang Y, Wang Y, Li B, Wang Z, Liu X, Zhang J, Ouyang Y. Structural behaviour  
790 of the aluminium alloy Temcor joints and Box-I section hybrid gusset joints under  
791 combined bending and shear. *Eng Struct*. 2021; 249: 113380.  
792 <https://doi.org/10.1016/j.engstruct.2021.113380>
- 793 [18] Liu H, Du P, Chen Z, Xu F. Mechanical properties of T-plate stiffened gusset joints

- 794 for aluminum alloy single layer two-way grid shells. *J Build Eng.* 2021; 44: 103249.  
795 <https://doi.org/10.1016/j.jobe.2021.103249>
- 796 [19]Liu H, Ding Y, Chen Z. Static stability behavior of aluminum alloy single-layer  
797 spherical latticed shell structure with Temcor joints. *Thin-Walled Struct.* 2017; 120:  
798 355-365.  
799 <https://doi.org/10.1016/j.tws.2017.09.019>
- 800 [20]Xiong Z, Guo X, Luo Y, Zhu S. Elasto-plastic stability of single-layer reticulated  
801 shells with aluminium alloy gusset joints. *Thin-Walled Struct.* 2017; 115: 163-175.  
802 <https://doi.org/10.1016/j.tws.2017.02.008>
- 803 [21]Xiong Z, Zhu S, Zou X, Guo S, Qiu Y, Li L. Elasto-plastic buckling behaviour of  
804 aluminium alloy single-layer cylindrical reticulated shells with gusset joints. *Eng*  
805 *Struct.* 2021; 242: 112562.  
806 <https://doi.org/10.1016/j.engstruct.2021.112562>
- 807 [22]Guo X, Zhu S, Liu X, Wang K. Study on out-of-plane flexural behavior of  
808 aluminum alloy gusset joints at elevated temperatures. *Thin-Walled Struct.* 2018;  
809 123: 452-466.  
810 <https://doi.org/10.1016/j.tws.2017.11.045>
- 811 [23]Xiong Z, Guo X, Luo Y, Zhu S, Liu J. Experimental and numerical studies on  
812 single-layer reticulated shells with aluminium alloy gusset joints. *Thin-Walled*  
813 *Struct.* 2017; 118: 124-136.  
814 <https://doi.org/10.1016/j.tws.2017.05.007>
- 815 [24]Design of aluminum alloy structures - part 1-2: structural fire design: EN1999-1-2  
816 Eurocode 9. Brussels: European Committee for Standardization; 2007.
- 817 [25]Ansys Inc. ANSYS® Multiphysics 19.0. Canonsburg, Pennsylvania, USA, 2018.
- 818 [26]Guo X, Xiong Z, Luo Y, Qiu L, Huang W. Application of the component method  
819 to aluminum alloy gusset joints. *Adv Struct Eng*, 2015; 18(11): 1931-1946.  
820 <https://doi.org/10.1260/1369-4332.18.11.1931>
- 821 [27]Zhu S, Guo X, Liu X, Gao S. The in-plane effective length of members in  
822 aluminum alloy reticulated shell with gusset joints. *Thin-Walled Struct.* 2018; 123:  
823 483-491.  
824 <https://doi.org/10.1016/j.tws.2017.10.033>
- 825 [28]Ministry of Construction of the People's Republic of China. Code for design of  
826 aluminium structures GB 50429-2007. Beijing: China Planning Press; 2012. (in  
827 Chinese)
- 828 [29]Hurley M J. NFPA SFPE Handbook of Fire Protection Engineering (fifth edition).  
829 New York: Springer; 2015.
- 830 [30]Fan F, Yan J, Cao Z. Stability of reticulated shells considering member buckling.



831 Journal of Constr Steel Res. 2012; 77: 32-42.  
832 <https://doi.org/10.1016/j.jcsr.2012.04.011>  
833 [31]Zhu S, Ohsaki M, Guo X. Prediction of non-linear buckling load of imperfect  
834 reticulated shell using modified consistent imperfection and machine learning. Eng  
835 Struct. 2021; 226: 111374.  
836 <https://doi.org/10.1016/j.engstruct.2020.111374>  
837 [32]Zhu S, Ohsaki M, Guo X, Zeng Q. Shape optimization for non-linear buckling load  
838 of aluminum alloy reticulated shells with gusset joints. Thin-Walled Struct. 2020;  
839 154:106830.  
840 <https://doi.org/10.1016/j.tws.2020.106830>  
841 [33]Mathworks. Statistics and Machine learning Toolbox User's Guide R2020a, 2020.